Map-Hash-Repeat: A Cloud Programming Pattern for Iterative Computation

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ABSTRACT

In this thesis we describe an initial exploration of the Map-Hash-Repeat pattern of cloud computation, in the context of the F# programming language and the MBrace cloud framework. Map-Hash-Repeat can be viewed as a generalization of the well-known MapReduce pattern, where a) the reduce phase is replaced by “hashing”, i.e., re-distribution of results over the node topology; b) both the map and the reduce phases are repeatedly iterated; and c) the final result is produced (possibly via a full reduce phase) upon reaching an iteration fixpoint.

This pattern seems to capture a general mode of computation, e.g., easily simulating iterative algorithms, in addition to traditional MapReduce functionality.

Our prototype is in a functional setting, using the F# programming language, and leverages an existing framework for cloud computation to encode the Map-Hash-Repeat pattern succinctly.

SUBJECT AREA: Cloud computations, iterative algorithms

KEYWORDS: MapReduce programming model, F#, MBrace cloud programming pattern
ΠΕΡΙΛΗΨΗ

Στα πλαίσια αυτής της πτυχιακής εργασίας περιγράφουμε μια αρχική εξερεύνησή του προτύπου Map-Hash-Repeat για επαναληπτικούς κατανεμημένους υπολογισμούς, με χρήση της προγραμματιστικής γλώσσας F# και του Mbrace framework. Το Map-Hash-Repeat αποτελεί μια γενικευμένη τροποποίηση του γνωστού προγραμματιστικού προτύπου Map-Reduce, όπου: 1) το reduce στάδιο αντικαθίσταται με διαμοιρασμό των αποτελεσμάτων στην τοπολογία των κόμβων, 2) το map και το reduce στάδιο επαναλαμβάνονται και 3) το τελικό αποτέλεσμα προκύπτει (πιθανώς από ένα reduce στάδιο) όταν φτάσουμε σε κάποιο σταθερό σημείο.

Το πρότυπο φαίνεται να υποστηρίζει ένα γενικότερο τύπο υπολογισμών, για παράδειγμα υλοποιεί απλούς επαναληπτικούς αλγόριθμους σε συνδυασμό με την κλασσική λειτουργικότητα του MapReduce. Το πρωτότυπο αυτό αποτελεί ένα λειτουργικό περιβάλλον, χρησιμοποιώντας την προγραμματιστική γλώσσα F#, και αξιοποιεί ένα ήδη υπάρχον framework για υπολογισμούς στο δίκτυο ώστε να υλοποιείται συνοπτικά το πρότυπο Map-Hash-Repeat πρότυπο.

ΘΕΜΑΤΙΚΗ ΠΕΡΙΟΧΗ: Υπολογισμοί στο δίκτυο, επαναληπτικοί αλγόριθμοι

ΛΕΞΕΙΣ ΚΛΕΙΔΙΑ: προγραμματιστικό μοντέλο MapReduce, F#, προγραμματιστικό μοντέλο MBrace
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1. Introduction

Map-Hash-Repeat is a cloud programming pattern for iterative computations. It evolves the MapReduce programming model and it is used to simulate iterative algorithms in an easy way where both map and reduce phases are iterated and the final result is obtained (via a reduce phase) once we reach a fixpoint. To elaborate this, a map phase takes place at first and then the reduce phase is replaced by a re-distribution of the previously computed results over the node topology. The same procedure goes on until reaching an iteration fixpoint.

The MapReduce programming model is used for processing and generating large data sets in a distributed way over several machines. A MapReduce program consists of a map phase which processes some input data and generates (“maps”) it to intermediate `<key, value>` pairs according to the user’s specifications and a reduce phase that takes a collection of intermediate `<key, value>` pairs and “reduces” them according to the same intermediate key, in order to produce the final result.

Our prototype implementation of the Map-Hash-Repeat programming pattern is based on the F# programming language in combination with the MBrace cloud computing model. F# is an open-source programming language. Primarily, F# is a functional language, but it also supports imperative, object-oriented and functional styles of programming. Some of the main features of the F# language which are used in our Map-Hash-Repeat implementation are: code quotations, asynchronous workflows, pattern matching, discriminated unions and recursion. We also used some of the basic features of the MBrace cloud computing framework which are the cloud workflows and the cloud refs.

MBrace is a cloud programming model/framework which introduces an expressive and integrated way of performing large-scale computations running in the cloud. With the help of the F# programming language, MBrace offers a declarative style for describing distributed computations using the F# computation expressions which specify parallelism patterns known as cloud workflows or monads and as a result it express many different kind of algorithmic patterns, such as MapReduce and other iterative algorithms.
2. Background

2.1 MapReduce

MapReduce [1] is a programming model for processing large data sets in a distributed manner over several machines (tasks). It is used to deal with problems that can be separated into smaller independent sub-problems and require operations on large data sets. Its concept is very simple and the main idea is that the initial problem is divided into sub-problems, which are being distributed over the topology into tasks. There is a boss who takes the initial input and distributes it to the workers. So, each worker tries to solve a part of the initial problem. When completed, the boss node collects all the solutions from each worker and combines them in some way to form the output, which will be the final result of the initial problem.

In more detail, the MapReduce framework consists of two user-specified basic procedures: Map() and Reduce(). During the "Map" step, the Map() function takes as input a series of <key_i,value_i> pairs and they are "mapped" into a collection of intermediate <ikey_j,ivalue_j> pairs that are being distributed to worker nodes. Then, in the "Reduce" step, each worker performs a computation ("reduce") over the data it received and then passes the result to the boss in a form of <okey_i,ovalue_i> pair. Finally, the boss node collects all data from the workers and produces the final output.

![MapReduce process](image)

Figure 1: MapReduce process

---

Figure 1 shows the map and the reduce phase. In Step1, the input data is split into key-value pairs and the Map() function takes these pairs as input. The output can be one or more intermediate key-value pairs, as Step 2 shows. In Step3, all intermediate key-value pairs are grouped by key and in the next step each unique key is being given to the reducer including all its values. Then, the reducer performs a computation over its values and returns one or more key-value pairs. In the end, all output pairs are collected by the framework. The most important element is that the model is ideal for parallel programming because each key-value pair can be computed independently.

One of the most common examples in MapReduce is the wordcount example. In this example, the goal is to count the number of occurrences of each word in a large set of documents. This problem can be easily implemented using the MapReduce programming model. The map function would split the input lines into words and then would emit a <word,1> pair for each word. Then the pairs with the same key are grouped together and are passed to the same worker for the reduce step. So, the reduce function takes a collection of <key,value> pairs and sums the values of the pairs that have the same key. Finally, the output pairs are in the form of <word,occurences> and are passed to the boss.

2.1.1 MapReduce-based Frameworks

There are many implementations of the MapReduce framework. One of them is the well-known Apache Hadoop [2] project. Hadoop is an open source MapReduce implementation written in Java. It is designed to solve big problems that require computationally extensive operations. These operations can be executed in parallel on a large number of independent machines. Hadoop uses its own distributed file-system called Hadoop Distributed File System (HDFS) to provide access to the data from all the servers.

2.1.2 Criticism of MapReduce

Despite the fact that many programmers support the idea of the MapReduce programming model, many people, mainly from the database community, claim that MapReduce represent a major step backwards. To support their view, they argue that MapReduce has a serious performance problem when it comes to access huge amount of data because it uses no indexes. Its techniques are nothing new and they are more than 20 years old. They also assert that MapReduce is missing some main features that are provided by any modern DBMS and it is not compatible with many DBMS tools. However, MapReduce suits well for processing huge amounts of unstructured data and enables data distribution over the network.
2.2 Programming in F#

2.2.1 Quoted Expressions

In F#, many applications need to know not only the structure of a block of source code but also the way it operates. In order to do that, F# provides a specially delimited expression which is called *quoted expression* so that the expression is compiled into an object which represents this expression. With this feature, the programmer can see the abstract syntax tree of the code. These quoted expressions can be executed then by alternative means such as an SQL query or as JavaScript in a client-side Web browser. In other words, this mechanism lets the programmer convert a computational representation of the program to an abstract syntax representation of the same language with which you can for instance analyse, execute, print or compile those programs in other ways.

Quoted expressions come in two ways: typed or untyped. To add type information, one can place the quotation markers `<@ @>` around an expression.

For example, the following code shows a typed quotation:

```
open Microsoft.Fsharp.Quotations
let expr1 : Expr<int> = <@ 1 + 1 @>
//val expr : Quotations.Expr<int> = Call (None, op_Addition, [Value (1), Value (1)])
```

As you see in the Table 1, the act of quoting an expression gives you back the expression as data. The generic type parameter `Expr<int>` is the result of the expression `<@ 1 + 1 @>` which in this example is an integer.

In order to obtain an untyped quotation, one can use the `@@ @@` quotation markers around an expression, as in the following example below:

```
open Microsoft.Fsharp.Quotations
let expr2: Expr = <@@ 1 + 1 @@>
//comment
//val expr : Quotations.Expr = Call (None, op_Addition, [Value (1), Value (1)])
```
In Table 2, the result Expr of the expression is not a generic type.

2.2.2 Asynchronous Workflows

Another important feature of the F# programming language are the asynchronous workflows [5]. With asynchronous workflows F# provides a programming model which enables the programmer to indicate which computations are going to be executed in the background threads in an asynchronous way as the execution continues on the current thread, without blocking it. For instance, background threads can perform different kinds of work such as responding to I/O requests, sleeping or waiting to acquire shared data. Asynchronous workflows avoid the need of explicit callbacks and the user writes the code as if it was executed sequentially.

To create asynchronous workflows, the code is wrapped in the async computation expression builder. A computation expression builder is an F# feature which lets the user define the characteristics of his own computation expression by creating a custom builder class and defining its methods. The syntax for defining a computation expression of type builder-name is builder-name { expression }. This type specifies code that controls the execution of the expression.

The result of an async computation is an Async<'T> object which can be thought of as an asynchronous computation that will compute a value type 'T. In order to begin an asynchronous operation the keywords let! (let-bang) and do! (do-bang) are being used. Within asynchronous workflow expressions, the language construct let! var= expr means “perform the asynchronous operation expr and bind the result to var when the operation completes. Then continue by executing the rest of the computations”. The difference between let and let! is that the first one just stores the result as an asynchronous operation, while the second executes the asynchronous operation and returns the data.

To start an asynchronous workflow, the simplest way is to use the Async.Start method which takes an Async<unit> as a parameter in order to begin the execution but in order for the async operation to return a value, the Async.RunSynchronously method is called immediately after the Async.Parallel method.

The Async.Parallel method takes a seq<Async<'T>> and starts to execute all the asynchronous computations in parallel, and then the Async.RunSynchronously method is called to initiate the execution of the asynchronous computations.

The following example shows how to use asynchronous workflows to fetch several Web pages in parallel.

Table 3: Fetching Web pages length asynchronously

| open System.IO |
open System.Net

let fetchAsync(name, url: string) =
    async {
        printfn "Request for %s" name
        let req = WebRequest.Create(url)
        let! resp = req.AsyncGetResponse()
        printfn "Response for %s" name
        let stream = resp.GetResponseStream()
        printfn "Reading response for %s" name
        let reader = new StreamReader(stream)
        let html = reader.ReadToEndAsync().Result
        printfn "Read %d characters for %s" html.Length name
        return (name,html.Length)
    }

Async.Parallel [for name, url in webPages -> fetchAsync(name, url)]
|> Async.Ignore
|> Async.RunSynchronously

The types of these functions are:

Table 4: Function return types

| val webPages : (string * string) list |
| val fetchAsync : name:string * url:string -> Async<string*int> |

Running the code in F# interactive, the output is:

Table 5: Output fetchAsync method

Request for yahoo
Request for google
Response for google
Reading response for google
Read 46800 characters for google
Response for yahoo
Reading response for yahoo
Read 91516 characters for yahoo

As one can see in Table 5, there are simultaneous web requests. The most important thing is that the threads which are responsible for these requests are not blocked.

At the example in Table 3, we use the namespaces System.IO and System.Net provided by the .NET framework for reading to data streams and using Internet resources easily. The
webPages function contains a list of tuples and the fetchAsync function takes as input two strings, a name and a url. The output is an Async<string*int> type object. The next three lines perform the execution of the program. The pipeline operator |> is defined as shown in Table 6.

Table 6: Pipeline operator

| let ( |> ) x f = f x |

The above operator it applies the first operand (x) to the function given in the second operand (f).

The Async.Parallel method creates an asynchronous computation and executes all the given fetchAsync computations in a fork/join pattern. This computation is passed to the Async.Ignore method, using the pipeline operator, to run and ignore its result. Finally, the RunSynchronously method executes in parallel all these sequence computations and awaits the result.

2.2.3 Pattern matching

Pattern matching is a very powerful and flexible feature of the F# programming language that is used to examine data structures and their values against one or more conditions. Instead of using series of if...then...else statements, F# offers the pattern matching. In general, patterns are used to compare data with a structure, or to decompose data into its parts or to extract information from structures. They are used in the match expression that has the following form:

Table 7: Match expression used for pattern matching

| match test-expression with |
| | pattern1 [when condition] -> result-expression1 |
| | pattern2 [when condition] -> result-expression2 |
| | ... |

In the form in Table 7, test-expression is the expression that will be matched. Most of F#’s types can be used as text-expressions. The pattern specifies how to deconstruct the text-expression. The when condition is optional. For a successful matching, the pattern must satisfy the test-expression and the when condition must evaluate to true. The result-expression is returned in a successful match. The patterns are tested one by one and the procedure stops once a match is found.

A simple example for matching constants is described.
In the above example, F# compares the test-expression 5 with the pattern 5 and considers the match as valid. Then, it evaluates the result-expression and returns the string “Match!”. As one can notice, the pattern 2 will never be tested. This means that the order of the patterns matters.

### 2.2.4 Discriminated unions

Discriminated unions are data types with a finite number of different representations. They can be though of as the union data type in C. The are defined using the keyword `type` followed by a name and then the union cases separated by the pipe symbol `|`. Discriminated unions have the following form:

Table 9: Discriminated union type

<table>
<thead>
<tr>
<th>type type_Name =</th>
</tr>
</thead>
<tbody>
<tr>
<td>Case1 [of datatype1] [* datatype2] ...</td>
</tr>
<tr>
<td>Case2 [of datatype3] [* datatype4] ...</td>
</tr>
<tr>
<td>...</td>
</tr>
</tbody>
</table>

For instance, a type is described below, which can me either an integer or a boolean.

Table 10: Example of the discriminated union type intOrBool

<table>
<thead>
<tr>
<th>type intOrBool =</th>
</tr>
</thead>
<tbody>
<tr>
<td>Int of int</td>
</tr>
<tr>
<td>Bool of bool</td>
</tr>
</tbody>
</table>
2.2.5 Reference Cells

A ref cell is used to hold a mutable value, meaning that the user can change it anytime. The ref operator is used before a value to allocate a new ref cell for the given value. To assign a new value to a reference cell one can use the assignment operator := and to read its contents one can use the ! (bang) operator, as the following example shows.

**Table 11: Reference cell example**

```fsharp
let r = ref 3
printfn "%d" !r
r := 5
printfn "%d" !r
```

In the above example we create a ref cell that contains the value 3 and then we change its value to 5.
To clarify this, reference cells point to a memory address. This means that if one has several ref cells pointing to the same address, changes at that memory address will affect all the ref cells pointing to it.

2.3 Programming in Mbrace

2.3.1 Concepts

The programming model of MBrace [3] is very similar to the form of the F# asynchronous workflows. Just as in asynchronous workflows one uses the syntax async { expression } to set up a computation expression that runs asynchronously, MBrace offers cloud workflows to introduce distributed computations. Their execution can be performed only within a distributed environment. The framework provides the MBrace runtime that provides an environment that abstractly distributes the execution of cloud computations. The environment handles quite good data distribution but when it comes to big data it is not so efficient. MBrace offers a mechanism to manage global data, known as cloud refs. In the following section these concepts are described in details.

2.3.2 Cloud Workflows

MBrace provides cloud workflows in order one to define distributed computations. Their style bears a strong resemblance to F# asynchronous workflows. In the same way that asynchronous workflows are scoped by the async { } builder and are being executed in
threads, cloud computations use the cloud \{\} expression builder known as cloud block and are being executed in a distributed way. Their execution is postponed until they are being sent to the MBrace runtime for evaluation. The type of a cloud computation is ICloud<T> and once executed, the output is of type T. All cloud blocks must be declared with the [Cloud] attribute.

The following example declares a simple computation.

**Table 12: Hello World example**

```ml
[Cloud]
let HelloWorld() =
    cloud {
        return "Hello world"
    }
```

In Table 12, one can see that this computation returns an ICloud<string> type. This result should be dereferenced in order to obtain the string type. To instantiate a local MBrace runtime, the user has to execute the following command:

**Table 13: A local MBrace runtime initialization**

```ml
let runtime = Mbrace.InitLocal 4
```

The code in Table 13 initializes a cluster of 4 nodes locally on the current machine. To execute a cloud computation, one can run the following code. The result is type of string with value “Hello world”.

**Table 14: Execution of the HelloWorld cloud computation**

```ml
Runtime.Run <@ HelloWorld() @>
```

We can now define the same example in Table 3 using cloud blocks as the following table shows.

**Table 15: Fetching Web pages length in parallel**

```ml
[Cloud]
let cloudFetchAsync() =
    cloud {
        let jobs =
            Array.map (Cloud.OfAsync << fetchAsync) webPages
```
let! results = Cloud.Parallel jobs
    return results

The *Array.map* function applies the given function to each element of the array and returns a new array.

This section explains some basic MBrace combinators that are used in the above example.

- **Cloud.OfAsync**

With this combinator, one can use asynchronous computation expressions inside cloud blocks. Its type signature is:

<table>
<thead>
<tr>
<th>Table 16: Type signature of Cloud.OfAsync combinator</th>
</tr>
</thead>
<tbody>
<tr>
<td>Async&lt;'a&gt; → ICloud&lt;'a&gt;</td>
</tr>
</tbody>
</table>

The combinator does not change the semantics of the *async* computation. It is useful when one needs to adjust existing asynchronous workflows in cloud workflows. For instance, we can use the *Cloud.OfAsync* combinator to embed the following asynchronous workflow, which causes the execution to stop for \(x\) milliseconds, in a cloud block.

<table>
<thead>
<tr>
<th>Table 17: Asynchronous workflow example</th>
</tr>
</thead>
<tbody>
<tr>
<td>let sleep x =</td>
</tr>
<tr>
<td>async {</td>
</tr>
<tr>
<td>do! Async.Sleep x</td>
</tr>
<tr>
<td>}</td>
</tr>
</tbody>
</table>

Then, the cloud computation is declared in Table 18.

<table>
<thead>
<tr>
<th>Table 18: Cloud computation expression with an embedded asynchronous workflow</th>
</tr>
</thead>
<tbody>
<tr>
<td>[&lt;Cloud&gt;]</td>
</tr>
<tr>
<td>let cloudSleep() =</td>
</tr>
<tr>
<td>cloud {</td>
</tr>
<tr>
<td>do! Cloud.OfAsync (sleep 3000)</td>
</tr>
<tr>
<td>}</td>
</tr>
</tbody>
</table>
• **Cloud.Parallel**

The Cloud.Parallel combinator is used to execute cloud computations in parallel. The signature of the type is:

**Table 19: Type signature of Cloud.Parallel combinator**

```
Cloud<'T> [] → Cloud<'T[]>
```

As one can see from the above table, the combinator takes as input an array of cloud computations and executes them in parallel. The result is an array containing the result of each computation. It is worth mentioning that each computation is allocated in different worker and is executed in a fork/join pattern. In other words, the boss waits until all the workers terminate and then joins the results to return the final result.

The following example shows the use of the Cloud.Parallel combinator.

**Table 20: Cloud.Parallel combinator example**

```
[<Cloud>]
let parallelExample() =
    cloud {
        let func x y = cloud {return x + y}
        let jobs = [|for i in 1 .. 1000 -> func i (i*i) |]
        let! results = Cloud.Parallel jobs
        return results
    }
```

The parallelExample cloud workflow creates 1000 cloud computations that are being executed in parallel using the Cloud.Parallel combinator and finally the results are being collected.

### 2.3.3 Cloud Refs

Cloud refs are very similar to F#’s reference cells but they are distributed and immutable by design. Once they are being declared, they require a real-time decision by the runtime as far as the locality and the load mechanism is concerned. The MBrace runtime uses some techniques, such as caching local copies to workers, to manage the values of the cloud refs and lessening duplicate copies of repeating data. The type of the cloud refs is ICloudRef<'T>, where 'T is the type of the contained value.
Using the `fetchAsync` function we defined in Table 3, one can create a cloud workflow to get the length of a web page, but this time a reference to the result will be returned that will contain the value instead of the actual value.

**Table 21: Using cloud refs to fetch the length of a web page**

```fsharp
let getRef() =
    cloud {
        let! jobs = Cloud.OfAsync <| fetchAsync ("google", "http://google.com")
        let! ref = CloudRef.New jobs
        return ref
    }
```

The `CloudRef.New` method creates a new cloud ref that contains the given value. The result of the `getRef` function is of type `ICloudRef<string*int>`, which is a reference to the result. To get the cloud ref, one can run:

**Table 22: Receive a cloud ref**

```fsharp
let cloudRef = runtime.Run <@ getRef() @>
```

In order to get the actual value of the above cloud ref, the programmer has to run the following line:

**Table 23: Dereferencing a cloud ref**

```fsharp
let data = cloudRef.Value
```

In the context of a cloud computation, the user can get the value of a cloud ref using the `CloudRef.Read` method. This method takes a cloud ref `ICloudRef<'a>` and returns a workflow `ICloud<'a>` that contains the enclosed value.

However, there is a mutable version of cloud refs; the `MutableCloudRef` type. The difference between the immutable and the mutable version is that a mutable cloud ref can update its contained value and it can be deallocated manually by the user. These imply that the values can not be cached. Mutable cloud refs usually are used to define user-specified data structures or to create synchronization mechanisms like semaphores. The type of the `MutableCloudRef` is `IMutableCloudRef<'T>`, where `'T` is the type of the contained value.

The following describes some useful functions that are used to manage the mutable cloud refs.

**Table 24: Functions that manage mutable cloud refs**

<table>
<thead>
<tr>
<th>Name</th>
<th>Type</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>MutableCloudRef.New</td>
<td><code>'a -&gt; ICloud&lt;ICloudRef&lt;'a&gt;&gt;</code></td>
<td>Takes a value and creates a</td>
</tr>
<tr>
<td>Method</td>
<td>Description</td>
<td></td>
</tr>
<tr>
<td>---------------------------------------</td>
<td>-----------------------------------------------------------------------------</td>
<td></td>
</tr>
<tr>
<td><strong>MutableCloudRef.Read</strong></td>
<td>IMutableCloudRef&lt;'a&gt; → ICloud&lt;'a&gt; Returns the value of the given MutableCloudRef.</td>
<td></td>
</tr>
<tr>
<td><strong>MutableCloudRef.Force</strong></td>
<td>IMutableCloudRef&lt;'a&gt;*'a → ICloud&lt;unit&gt; It tries to update the value of the given MutableCloudRef with the given value without checking if it was updated by someone else.</td>
<td></td>
</tr>
<tr>
<td><strong>MutableCloudRef.Set</strong></td>
<td>IMutableCloudRef&lt;'a&gt;*'a → ICloud&lt;bool&gt; It tries to update the given MutableCloudRef with the given value and returns true if on success. If its value has been modified since the last time that it was read it returns false.</td>
<td></td>
</tr>
<tr>
<td><strong>MutableCloudRef.SpinSet</strong></td>
<td>IMutableCloudRef&lt;'a&gt;*('a → 'a) → ICloud&lt;unit&gt; It updates a MutableCloudRef using the function given in the second argument.</td>
<td></td>
</tr>
</tbody>
</table>

### 2.3.4 MapReduce in Mbrace

The MBrace framework provides a library that one can define and execute MapReduce tasks. The recursive mapReduce method is very simple. It takes a user-specified map and reduce function, an identity value to be used as a termination condition and a list with the input values. The algorithm splits, if needed, the input into halves and passes each half in two mapReduce calls and executes them in parallel.

**Table 25: mapReduce library in MBrace**

```ocaml
<Cloud>
let rec mapReduce (map : 'T -> ICloud<'R>)
  (reduce : 'R -> 'R -> ICloud<'R>)
  (identity : 'R)
  (input : 'T list) =
cloud {
  match input with
  | []      -> return identity
  | [value] -> return! map value
  | _       ->
    let left,right = List.split input
    let! r1,r2 =
      (mapReduce map reduce identity left)
    <||>
  }
```
In the above code, the \textit{List.split} method is an Mbrace function that takes a list and splits it in half, returning the two new lists in a tuple. The \textit{parallel decomposition operator} \texttt{<||>} is an abbreviation of the \textit{Cloud.Parallel} combinator but only for a 2-dimensional array as input.
3. Map-Hash-Repeat

3.1 Overview

Map-Hash-Repeat is a programming pattern for supporting iterative computations in the cloud. Its main idea is based on the MapReduce programming model but there are differences in how the reduce phase is defined as well as in the computation of the final output. Map-Hash-Repeat requires an initial node topology in memory to apply the pattern. This limitation is necessary because the algorithm needs an initial input to generate the final solution in the next iterations. Once this has been done, the algorithm executes iteratively two main steps: the first being a map step that is similar to MapReduce's map and a second being the reduce step defined in a different manner. During the map phase, intermediate values are computed in one step. The reduce phase that follows is different from that in MapReduce: instead of reducing these values, these are being distributed over the topology. The concept is that during the n^{th} iteration the algorithm uses the values computed during the previous iteration to compare them with the new ones. The algorithm terminates once in all nodes the previous computed value and the new one are the same.

This implies that each node has to keep the value it computed in the previous iteration. Once all nodes terminate, the iteration stops and the output is produced. In the meantime, the node topology can change appropriately according to the newly computed values. The importance of this redistribution is the fact that the new topology is based on the newly computed values, which helps the algorithm to converge faster.
While the old and the new values are different

Map(): compute intermediate values

Distribute the Intermediate values

Change node topology

Compare the old with the new values

Final result

Figure 2: Iterative Map-Hash-Repeat programming model
3.1.1 Description of the algorithm

The following algorithm describes the Map-Hash-Repeat programming pattern.

Table 26: MapHashRepeat pseudocode

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>computeValues :=</td>
<td>computes the new values that will be used for the next iterations</td>
</tr>
<tr>
<td>createNewTopology:=</td>
<td>creates a new topology according to the already computed values</td>
</tr>
<tr>
<td>keepPrevState :=</td>
<td>swap the prevValue with the newValue</td>
</tr>
</tbody>
</table>

```plaintext
function recursive mapHashRepeat(input1, input2) :
    newValues := computeValues(input1,input2);
    for each node n in input2:
        n.Values := add(newValues[n]);
        newTopology := createNewTopology(input1,input2);
    //returns an array of boolean values, one from each node, on whether
    //the previous value equals the new one or not
    states :=
        [for each node n in input2:
            prevValue := n.getPrev;
            newValue := newTopology[n];
            keepPrevState(prevValue,newValue,n);
            if newValue == prevValue:
                return true;
            else:
                return false;
        ]
    finalState := true;
    for each state s in states:
        finalState := state && true;
    if finalState == true:
        return (input1,input2);
    else:
        mapHashRepeat(input1,input2);
```

3.1.2 Programming Interface

To simulate an iterative algorithm in the Map-Hash-Repeat programming model one should define some user specified functions that are used during the execution of the main algorithm.
The following table describes these functions.

<table>
<thead>
<tr>
<th>Name</th>
<th>Type</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>createNodes</td>
<td>int-&gt;int → ICloud&lt;IMutableCloudRef&lt;Node&lt;int,(float*float),Set&lt;int&gt;&gt;&gt; []</td>
<td>This function is used to create and distribute the initial data to the MBrace workers. The user needs to pass as arguments the number of the initial data and the number of the clusters. With the help of the cloud refs, offered by the MBrace programming model, this function returns a cloud computation of an array that contains references of the data and the center nodes. Dereferencing these computations, one can get the values of the data and the center nodes. Each node is of type Node.</td>
</tr>
<tr>
<td>createNeighbors</td>
<td>IMutableCloudRef&lt;Node&lt;int,(float<em>float),'oldV&gt;&gt; [] -&gt; ICloud&lt;IMutableCloudRef&lt;Node&lt;int,(float</em>float),'oldV&gt;&gt; [] <em>IMutableCloudRef&lt;Node&lt;int,(float</em>float),'oldV&gt;&gt; []</td>
<td>This function takes as an input the cloud references of two arrays of type Node. The goal is to create an initial topology. The output is a tuple in a cloud computation which contains the cloud references of both inputs.</td>
</tr>
<tr>
<td>compute</td>
<td>IMutableCloudRef&lt;Node&lt;int,(float<em>float),'oldV&gt;&gt; [] → IMutableCloudRef&lt;Node&lt;int,(float</em>float),'oldV&gt;&gt; [] → ICloud&lt;unit []&gt;</td>
<td>This function is used to calculate the computation that will be used in the future iterations of the algorithm. It takes as parameters the cloud references of two arrays of type Node.</td>
</tr>
<tr>
<td>computeNeighbors</td>
<td>IMutableCloudRef&lt;Node&lt;&lt;Id,(float<em>float),'oldV&gt;&gt; [] → IMutableCloudRef&lt;Node&lt;&lt;Id,(float</em>float),'oldV&gt;&gt; [] → ICloud&lt;Map&lt;&lt;Id,Set&lt;int &gt;&gt;&gt;</td>
<td>This function takes as input two arrays of type Node and calculates the new topology in the future iterations. It returns a mapping specifying how the new topology is defined.</td>
</tr>
</tbody>
</table>
5. isDone IMutableCloudRef<Node<Id, 'newV', 'oldV'> >→ Set<Id> → ICloud<bool>

This function is used to check whether we reach a fixpoint or not. It takes as input a cloud reference of type Node and a set of values and checks if the previous computed values are the same with the old ones and returns a boolean value.

3.2 Examples

3.2.1 K-means

K-means is an algorithm which is used to identify the best way to partition a specific dataset into \( k \) clusters in which the distance between each member of the cluster and the cluster's centroid is the minimum. The user specifies a set of input data and the number \( k \) of the clusters to be created. Each element in the input data can be a d-dimensional array. The main idea is that \( k \) initial centroids are randomly defined and then \( k \) clusters are being created. Then, each element in the dataset is assigned to the cluster with the closest centroid. For each cluster, the algorithm recalculates the centroids and all the elements are reassigned to the clusters depending on the new centroid values. The same procedure is repeated until the elements can no longer change clusters.

K-means always converges in polynomial time but it is important to mention that it does not always find the optimal solution. Also, despite the fact that K-means clustering is an NP-hard problem, there are heuristic methods which can be used in order for the algorithm to converge in polynomial time.

3.2.2 Map-Hash-Repeat implementation of K-means

The Map-Hash-Repeat cloud programming pattern can simulate easily iterative algorithms, one of them is K-means, which was described above. In our example, for the sake of simplicity, 2-dimensional points are used for the implementation of the K-means algorithm using the Map-Hash-Repeat pattern. The basic idea is to distribute the elements from the dataset to MBrace workers and then execute the K-means algorithm in order to define the final clusters. In this section the K-means algorithm is described in terms of Map-Hash-Repeat terminology:

The dataset is a generic data type and is defined as a discriminated union Node which can have the value N with the following set of fields:

- a node identifier 'Id
- a type parameter 'value1 which will keep the coordinates of the points
- another type parameter 'value2 which keeps the set of nodes that were in the cluster in
the previous iteration in order to be checked with the new one and determine if it has been changed

- a set of identifiers Set<'Id> which keeps the identifiers of the nodes that are closest to the center node

As mentioned, in order to enable execution specific to K-means, one should define the functions in the Table 27. These functions are described in Table 28.

**Table 28: Map-Hash-Repeat user specified functions specially for K-means**

<table>
<thead>
<tr>
<th>Name</th>
<th>Type</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. createNodes</td>
<td>int-&gt;int → ICloud&lt;IMutableCloudRef&lt;Node&lt;int,(float * float),Set&lt;int&gt;&gt;&gt;[]&gt;</td>
<td>The user needs to pass as arguments the number of the initial data and the number of the clusters. This function returns a cloud computation of an array that contains references of the data and the center nodes. Dereferencing these computations, one can get the values of the data and the center nodes. Each node is of type Node. The first field is a unique identifier. In order to distinguish the data nodes from the centers, the identifiers of the latter are negative numbers. The second field is a tuple of two floats that specify the coordinates of the corresponding node. The last two fields are both empty sets.</td>
</tr>
<tr>
<td>2. createNeighbors</td>
<td>IMutableCloudRef&lt;Node&lt;int,(float*float),'oldV&gt;&gt;[]&gt; → ICloud&lt;IMutableCloudRef&lt;Node&lt;int,(float * float),'oldV&gt;&gt;[]&gt; *IMutableCloudRef&lt;Node&lt;int,(float * float),'oldV&gt;&gt;[]&gt;</td>
<td>This function takes as input the cloud references of the data nodes and the center nodes. Firstly, it separates the data from the centers of the first input parameter and then it calculates the euclidean distance between each data element and each center. After finding the closest center node for each data node, the function updates the values of the centroids by adding the identifier of the closest data node in the set of the identifiers of the corresponding center. The output is a tuple in a cloud computation which contains the cloud references of both data nodes and the updated centers.</td>
</tr>
<tr>
<td>3. compute</td>
<td>IMutableCloudRef&lt;Node&lt;int,(float * float),'oldV&gt;&gt;[]&gt; → IMutableCloudRef&lt;Node&lt;int,(float * float),'oldV&gt;&gt;[]&gt;</td>
<td>This function takes as parameters the cloud references of the data nodes and the centers. Then, for every center, it takes the coordinates of the nodes who are closest to it and calculates the new centroids which will be the</td>
</tr>
<tr>
<td>Function</td>
<td>Parameters</td>
<td>Description</td>
</tr>
<tr>
<td>--------------------------------</td>
<td>----------------------------------------------------------------------------</td>
<td>--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------</td>
</tr>
<tr>
<td>4. computeNeighbors</td>
<td>IMutableCloudRef&lt;Node&lt;'Id,(float*float),'oldV&gt;&gt; [] → ICloud&lt;T&gt;</td>
<td>This function takes as input parameters the cloud references of the data nodes and the centers and calculates the euclidean distance between each data node from all the centers. From all these calculations, the function gets the one with the minimum value and associates the data node to the closest center. Finally, it returns a mapping of each center identifier as a key and a set of identifiers of the closest data nodes to this specific center as a value.</td>
</tr>
<tr>
<td>5. isDone</td>
<td>IMutableCloudRef&lt;Node&lt;'Id,'newV,'oldV&gt;&gt; → Set&lt;'Id&gt; → ICloud&lt;bool&gt;</td>
<td>This function checks whether the cluster has been changed or not. It takes as input a center node and a set of identifiers. These identifiers belong to the data nodes which are closest to the given center. If the current set of the identifiers of the center is the same as the given set, then the function returns true, otherwise false.</td>
</tr>
</tbody>
</table>

Once one has defined the previous functions, the recursive “mapHashRepeat” function is invoked by the Map-Hash-Repeat framework which takes cloud references of the data nodes and the centers alongside with the functions 3,4,5 from Table 28 as input parameters in order to execute the internal algorithm. In every iteration the algorithm calculates the new centroids using the “compute” function and then assigns each node the closest center using the “computeNeighbors” function. In the next step for each center the algorithm checks whether the new set of the identifiers of the closest nodes which it calculated before is the same as the old one or not. If the two sets are the same then a boolean value “true” is stored in an array, otherwise a boolean value “false” is stored. Finally, the array contains as many boolean value as the number of the center nodes and if all these values are true it means that the clusters no longer change and the algorithm terminates returning the data nodes and the center nodes. On the other hand, if even one of the values is false the “mapHashRepeat” function is called with the new computations and the same procedure is followed.

In Appendix I, one can see the full implementation of the K-means algorithm in the Map-Hash-Repeat pattern.

### 3.3 Implementation

Our implementation of the Map-Hash-Repeat programming model is based on the F# programming language and the Mbrace cloud framework. The main reason why we chose
this programming language is because the Mbrace framework is written in F# and takes advantage of many of the language features. Also, many common programming tasks, like list processing, are much more simpler in F#. The following table shows the implementation of the Map-Hash-Repeat programming model in F#.

<table>
<thead>
<tr>
<th>Table 29: Map-Hash-Repeat programming model</th>
</tr>
</thead>
</table>

```fsharp
let rec mapHashRepeat (input1 : IMutableCloudRef<Node<'Id,'newV,'oldV>> [])
    (input2 : IMutableCloudRef<Node<'Id,'newV,'oldV>> [])
    (computeValues : (IMutableCloudRef<Node<'Id,'newV,'oldV>> [] ->
        IMutableCloudRef<Node<'Id,'newV,'oldV>> [] ->
        ICloud<Map<'I,'C>>)
    )
 createNewTopology
 isDone = cloud {
    let keepPrevState (node : IMutableCloudRef<Node<'Id,'newV,'oldV>> ) newV = cloud {
        let! cloudNode = MutableCloudRef.Read(node)
        match cloudNode with
            | N(v1,v2,oldSet,currentV)  ->
                let newData = (v1,v2,currentV,newV)
                do! MutableCloudRef.Force(node,N(newData))
    }

    let! newValues = computeValues input1 input2
    let distribute = Array.map (fun input -> cloud {
        let! cloudInput = MutableCloudRef.Read(input)
        match cloudInput with
            | N(v1,v2,oldV,newV)  ->
                do! MutableCloudRef.Force(input,N(v1,newValues.[v1],oldV,newV))
    }) input2
    let! _ = distribute |> Cloud.Parallel

    let! newT opology = createNewT opology input1 input2
    let checkAll = |
        for input in input2 -> cloud {
            let! cloudInput = MutableCloudRef.Read(input)
            match cloudInput with
                | N(v,_,_,_) when Map.containsKey (v) newT opology  ->
                    let comp = newT opology .[v]
                    let! ok = isDone input comp
                    do! keepPrevState input comp
                    return ok
        } |
    let! check = Cloud.Parallel checkAll
```

A. Kalogeropoulos
let fixpoint = check |> Seq.fold (fun acc item -> acc && item) true
match fixpoint with
  | true -> return (input1,input2)
  | false ->
    return! mapHashRepeat input1 input2 computeValues createNewTopology isDone

The programming model requires an initial node topology to apply the above function. The
algorithm applies the user-specified computeValues function to the input lists and then
distributes in parallel the new values to the second input list each time to the appropriate
element. A new node topology is created using the user-specified createNewTopology
function according to these new values. Afterwards, each element from the second input is
checked in parallel to determine whether its value computed in the \( n^{th} \) iteration is the same
as the new value, or not. An array of boolean values is created that contains one value for
each element from the input2. This value is true if the previous value equals the new one,
otherwise is false. At the same time, the new value is stored in the element for future
iterations. Finally, the array is “reduced” by applying the boolean and operation to each
element and returns an accumulator of the results. If the value of the accumulator is true, it
means that we reached a fixpoint. Otherwise, the next iteration begins by calling the again the
mapHashRepeat function.

The seq.fold function is used to determine whether we reached a fixpoint or not. It takes a
function, an accumulator and a sequence of elements and applies the given function to each
element while keeping each time the result in an accumulator. Its type is declared below.

<table>
<thead>
<tr>
<th>Table 30: Seq.fold method</th>
</tr>
</thead>
<tbody>
<tr>
<td>Seq.fold : ('State -&gt; 'T -&gt; 'State) -&gt; 'State -&gt; seq&lt;'T&gt; -&gt; 'State</td>
</tr>
</tbody>
</table>

### 3.4 Related Work

There are many improved implementations based on the well-known MapReduce
programming model but not many of them support iterative computations in the cloud. Twister
[4] is a MapReduce runtime, implementing a programming model that supports iterative
MapReduce computations in an efficient way. Twister separates the data into two types: static
and dynamic. Static data is used in every iteration and remains the same in each computation
while the dynamic data are the output of every iteration and in many algorithms are used in
the next iteration. Instead of reloading the static data in each iteration, Twister introduces a
new “configure” step to load the static data to the map/reduce tasks using long running
(cacheable) map/reduce tasks that exist during each computation. There is also an optional
reduction phase known as “combine”, which one can use to combine the results from all the
reduce tasks in a single value.
4. Conclusion and Future Work

In this thesis we introduced the Map-Hash-Repeat cloud programming pattern for iterative computations, which is relevant to the well-known MapReduce pattern. Our implementation is based on the F# programming language and the MBrace programming model. We have discussed the basic concepts of the MapReduce programming model and the main features of the F# programming language that were used in our prototype in combination with some of the features of the MBrace framework. We have also presented in details the Map-Hash-Repeat algorithm and its concepts and then we discussed the K-means algorithm and its implementation using the Map-Hash-Repeat programming pattern.

In the future, we plan to create a library that will provide the support to develop more iterative algorithms using the Map-Hash-Repeat programming model.
## Abbreviations

<table>
<thead>
<tr>
<th>Abbreviation</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>HDFS</td>
<td>Hadoop Distributed File System</td>
</tr>
<tr>
<td>SQL</td>
<td>Structured Query Language</td>
</tr>
<tr>
<td>DBMS</td>
<td>Database Management System</td>
</tr>
</tbody>
</table>
Appendix I

Here we implement the K-means algorithm using the Map-Hash-Repeat programming pattern.

```ocaml
type Node<'Id,'newV,'oldV when 'Id : comparison and 'oldV : comparison> =
  | N of 'Id*'newV*'oldV* Set<'Id>

[<Cloud>]
let rec seqMap (f : 'T -> ICloud<'S>) (inputs : 'T list) : ICloud<'S list> =
  cloud {
    match inputs with
    | [] -> return []
    | x :: xs ->
      let! v = f x
      let! vs = seqMap f xs
      return v :: vs
  }

[<Cloud>]
let createNodes (numData : int) (k : int) = cloud {
  let rnd = System.Random()
  let! initVals = [
    for i in 1..numData ->
      MutableCloudRef.New(N((1,(rnd.Next(0,11) |> float,rnd.Next(0,11) |> float),(Set.empty : int Set),Set.empty)))] |> Cloud.Parallel
  let! initCenters =
    [|for i in 1..k ->
      MutableCloudRef.New(N((-i,(rnd.Next(0,11) |> float,rnd.Next(0,11) |> float),(Set.empty : int Set),Set.empty)))] |> Cloud.Parallel
  return Array.append initVals initCenters
}

[<Cloud>]
let createNeighbors (nodes : IMutableCloudRef<Node<'Id,'newV,'oldV>> []) = cloud {
  //find the centers (nodes with id < 0)
  let! getCenters =
    [|for node in nodes ->
      cloud {
        let! cloudNode = MutableCloudRef.Read(node)
        match cloudNode with
        | N(id,_,_,_) when id < 0 ->
          return Some node
        | N(id,_,_,_) ->
          return None
      }|]|>
    Cloud.Parallel
  return Array.append initVals initCenters
}
```
let centers =
    getCenters
    |> Array.choose (fun x -> match x with
        | Some(ref) -> Some ref
        | None -> None)

let! getNodes =
    [for node in nodes -> cloud {
        let! cloudNode = MutableCloudRef.Read(node)
        match cloudNode with
            | N(id,_,_,_) when id > 0->
                return Some node
            | N(id,_,_,_) ->
                return None
    }]
    |> Cloud.Parallel

let dataNodes =
    getNodes
    |> Array.choose (fun x -> match x with
        | Some(ref) -> Some ref
        | None -> None)

//distance
let dist (x1, y1) (x2, y2) : float =
    let xDistance = x1 - x2
    let yDistance = y1 - y2
    xDistance * xDistance + yDistance * yDistance

//get the coordinates of the centers
let! centerCoords =
    [for center in centers -> cloud {
        let! cloudNode = MutableCloudRef.Read(center)
        match cloudNode with
            | N(id,coords,_,_) ->
                return (id,coords)
    }]
    |> Cloud.Parallel

//calculate distances between each node and each center and return (centerId,minDistance) pairs
let! minPairs =
    [for node in dataNodes -> cloud {
        let! cloudNode = MutableCloudRef.Read(node)
        match cloudNode with
            | N(_,coord,_,_) ->
                return (Array.map (fun (id,c) -> (id,dist c coord)) centerCoords) |> Array.minBy snd
    }]
    |> Cloud.Parallel

//create clusters
let addN pairMap = cloud {
    match pairMap with
        | (nodeId,clusterId) ->
            for center in centers do
                let! cloudNode = MutableCloudRef.Read(center)
                match cloudNode with
                    | N(id,newv,oldSet,newSet) when id = clusterId ->
                        return (nodeId, clusterId)
        | None ->
            return None
}

//centers
let centers =
    getCenters
    |> Array.choose (fun x -> match x with
        | Some(ref) -> Some ref
        | None -> None)

let! getNodes =
    [for node in nodes -> cloud {
        let! cloudNode = MutableCloudRef.Read(node)
        match cloudNode with
            | N(id,_,_,_) when id > 0->
                return Some node
            | N(id,_,_,_) ->
                return None
    }]
    |> Cloud.Parallel

let dataNodes =
    getNodes
    |> Array.choose (fun x -> match x with
        | Some(ref) -> Some ref
        | None -> None)

//distance
let dist (x1, y1) (x2, y2) : float =
    let xDistance = x1 - x2
    let yDistance = y1 - y2
    xDistance * xDistance + yDistance * yDistance

//get the coordinates of the centers
let! centerCoords =
    [for center in centers -> cloud {
        let! cloudNode = MutableCloudRef.Read(center)
        match cloudNode with
            | N(id,coords,_,_) ->
                return (id,coords)
    }]
    |> Cloud.Parallel

//calculate distances between each node and each center and return (centerId,minDistance) pairs
let! minPairs =
    [for node in dataNodes -> cloud {
        let! cloudNode = MutableCloudRef.Read(node)
        match cloudNode with
            | N(_,coord,_,_) ->
                return (Array.map (fun (id,c) -> (id,dist c coord)) centerCoords) |> Array.minBy snd
    }]
    |> Cloud.Parallel

//create clusters
let addN pairMap = cloud {
    match pairMap with
        | (nodeId,clusterId) ->
            for center in centers do
                let! cloudNode = MutableCloudRef.Read(center)
                match cloudNode with
                    | N(id,newv,oldSet,newSet) when id = clusterId ->
                        return (nodeId, clusterId)
        | None ->
            return None
Map-Hash-Repeat: A Cloud Programming Pattern for Iterative Computation

let! _ =
  minPairs
  |> Array.mapi (fun i (clusterId,minDist) -> (i+1,clusterId))  //node i will be added to cluster with id x
  |> Array.toList
  |> seqMap addN

return (dataNodes,centers)

//compute the new centers
[<Cloud>]
let compute (nodes : IMutableCloudRef<Node<'Id,'newV,'oldV>> [])
  (centers : IMutableCloudRef<Node<'Id,'newV,'oldV>> [])  = cloud {

  let newVals (center : IMutableCloudRef<Node<'Id,'newV,'oldV>> ) = cloud {
    //get the refs of the nodes who belong to the center
    let getNeighbors (center : IMutableCloudRef<Node<'Id,'newV,'oldV>> ) = cloud {
      let! cloudNode = MutableCloudRef.Read(center)
      match cloudNode with
      | N(_,_,_,setN) ->
        let neighborIds = Set.toList setN
        return [for n in neighborIds -> nodes.[n-1]]
    }
    //get the coordinates (2nd element) of the given node
    let getCoords (node : IMutableCloudRef<Node<'Id,'newV,'oldV>> ) = cloud {
      let! cloudNode = MutableCloudRef.Read(node)
      match cloudNode with
      | N(_,coords,_,_)  ->
        return coords
    }
    //get neighbors REFS from the given center
    let! neighborRefs = getNeighbors center
    //concatenate given center's coordinates with the neighbors' coordinates and return a list with tuples:
    (nodeId,coordinates)
    let! cloudNode = MutableCloudRef.Read(center)
    match cloudNode with
    | N(id,_,_,_) ->
      let! clusterCoords = seqMap getCoords neighborRefs
      return (id, clusterCoords)
  }
  //for each cluster, returns a list with the coordinates which will calculate the new center
  let! allCoords =
  [|for center in centers -> newVals center|]
  |> Cloud.Parallel
  //calculates the x coordinate for each new center
  let xs =
  Array.map (fun (id,coords) -> let xSum = List.fold (fun acc (x,y) -> acc + x) 0.0 coords
    xSum/coords.Length |> float) allCoords
  //calculates the y coordinate for each new center
  let ys =
  Array.map (fun (id,coords) -> let ySum = List.fold (fun acc (x,y) -> acc + y) 0.0 coords
    ySum/coords.Length |> float) allCoords

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let newCenters =
    Array.map2 (fun i x y  -> (-(i+1),(x,y))) xs ys
    |> Map.ofArray

    return newCenters

let computeNeighbors (dataNodes : IMutableCloudRef<Node<'Id,'newV,'oldV>> [])
    (centers : IMutableCloudRef<Node<'Id,'newV,'oldV>> [])
    = cloud {

    let dist (x1, y1) (x2, y2) : float =
        let xDistance = x1 - x2
        let yDistance = y1 - y2
        xDistance * xDistance + yDistance * yDistance

    //get the coordinates of the centers
    let! centerCoords =
        [|for center in centers -> cloud {
            let! cloudNode = MutableCloudRef.Read(center)
            match cloudNode with
            | N(id,coords,_,_) ->
                return (id,coords)
        }|]
        |> Cloud.Parallel

    //calculate distances between each node and each center and returns (centerId,minDistance) pairs
    //first pair is for node with id = 1, second pair for node with id = 2 etc.
    let! minPairs =
        [| for node in dataNodes -> cloud {
            let! cloudNode = MutableCloudRef.Read(node)
            match cloudNode with
            | N(_,coord,_,_) ->
                return (Array.map (fun (id,c) -> (id,dist c coord)) centerCoords) |> Array.minBy snd
        }|]
        |> Cloud.Parallel

    //returns a list with (cld,nid) which means that
    //node with id nid belongs to cluster with id cld
    return
        minPairs
        |> Array.mapi (fun i (cld,minDist)  -> (i+1,cld) )
        |> Seq.groupBy snd |> Seq.map (fun (cld,seqnIds) -> (cld, (Seq.map (fun (nid,cid) -> nid) seqnIds) |> Set.ofSeq ))
        |> Seq.toArray
        |> Map.ofArray

let rec mapHashRepeat (dataNodes : IMutableCloudRef<Node<'Id,'newV,'oldV>> [])
    (centers : IMutableCloudRef<Node<'Id,'newV,'oldV>> [])
    (calcCenters : IMutableCloudRef<Node<'Id,'newV,'oldV>> []) ->
        IMutableCloudRef<Node<'Id,'newV,'oldV>> [] ->
        ICloud<Map<'I,'C>>))
    computeNeighbors
isDone  = cloud {

[<Cloud>]

let changeV (node : IMutableCloudRef<Node<'Id,'newV,'oldV>> ) comp = cloud {
    let! cloudNode = MutableCloudRef.Read(node)
    match cloudNode with
    | N(id,coords,oldSet,currentV)  ->
        let newData = (id,coords,currentV,comp)
        do! MutableCloudRef.Force(node,N(newData))

    let! newCenters = calcCenters dataNodes centers

    let distribute =
        [|for center in centers -> cloud {
            let! cloudNode = MutableCloudRef.Read(center)
            match cloudNode with
            | N(id,coords,oldSet,newSet)  ->
                do! MutableCloudRef.Force(center,N(id,newCenters.[id],oldSet,newSet))
        }|]
    |> Cloud.Parallel

    let! neighborPairs = computeNeighbors dataNodes centers

    let checkAll =
        [|for node in centers -> cloud {
            let! cloudNode = MutableCloudRef.Read(node)
            match cloudNode with
            | N(id,_,_,_) when Map.containsKey (id) neighborPairs ->
                let comp = neighborPairs.[id]
                let! ok = isDone node comp
                do! changeV node comp
                return ok
        }|]
    |> Cloud.Parallel

    let ok = check |> Seq.fold (fun acc item -> acc && item) true
    match ok with
    | true -> return (dataNodes,centers)
    | false ->
        return! mapHashRepeat dataNodes centers calcCenters computeNeighbors isDone //(ref true)

    [<Cloud>]
    let isDone (node : IMutableCloudRef<Node<'Id,'newV,'oldV>> ) comp = cloud {
        let! cloudNode = MutableCloudRef.Read(node)
        match cloudNode with
        | N(id,coords,setN,currentSet) -> return currentSet = comp
    }

    let runtime = MBrace.InitLocal 4
    //number of data points, number of clusters
    let allNodes = runtime.Run <@ createNodes 7 2 @>
    let (nodes,centers) = runtime.Run <@ createNeighbors allNodes @>
    let (finalNodes,finalCenters) = runtime.Run <@ mapHashRepeat nodes centers compute computeNeighbors isDone @>
References


